

## STUDYING THE THERMALLY POLLUTED MIXING ZONE SIZE IN OPEN CHANNELS

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### ABSTRACT

This work investigates experimentally the characteristics of the thermal area of pollution resulting from surface discharge outfalls of the steam electrical power plant cooling system. The experimental program was carried out in a rectangular flume inside the northern experimental hall of the Hydraulics Research Institute (HRI) in Egypt. The flume has dimensions of 17.8 m length, 2.5 m width, and 0.5 m deep. Formulae and curves to identify the mixing zone center-line length for different outfall angles were developed. The predicted formulae could be used in the cooling system surface discharge design phase to predict the minimum dilution of the thermal plume at different discharge rates in Egypt. The predicted formulae could also help in updating the environmental and water legislations in Egypt.

تهدف هذه الرسالة إلى الوصول إلى فهم أعمق لظاهرة التبادل الحراري في القنوات المائية الناتجة من محطات توليد الطاقة الكهربائية مما يتسبب في حدوث تلوث حراري يؤثر على البيئة وعلى الأحياء المائية. وفي هذه الدراسة تم دراسة المجال القريب لتحديد طول محور منطقة الخلط وتعريفها من الناحية العملية والحسابية. وقد تم تغيير بعض العوامل وحساب تأثيرها على منطقة الخلط مثل رقم فرود ومعامل السرعة ومعامل الطول على نصف العرض كل ذلك عند زاويتي مخرج (30°، 60°). ولتحقيق هذه الدراسة تم إنشاء نموذج مصغر لقناة بعرض 2.5 متر وطول 17.8 متر ونصف متر عمق. وتم استنتاج معادلات تصميمية تطبيقية لحساب طول المحور ولقد تم استنتاج معادلة لحساب طول المحور عند زاوية مخرج تساوي 90° كذلك التي استنتجها ميلر بنفس العوامل (رقم فرود، معامل الارتفاع على نصف العرض) مع إضافة معامل السرعة للمعادلة مما يتيح إستخدامها للمياه الساكنة أو المتحركة وقد أعطت توافق جيد معه.

في النهاية قد تبين من تطبيق هذه المعادلات على بعض محطات الكهرباء في مصر انها أداة جيدة عند لتوقع طول المحور لمنطقة الخلط بما يناسب ظروف المحطة ومصدر المياه وبما تقتضيه قوانين المنطقة.

**Keywords:** Mixing zone center line, outfall angle, near field, thermal discharge, temperature, Densimetric Froude Number and aspect ratios

### 1. INTRODUCTION

Egypt has the highest population in the Arab World. Egypt had an installed electric generating capacity of 18.936 giga-watts in 2006/2007 with plans to raise the capacity to more than 23.0 giga-watts by year 2010. About 73% of Egypt's electric generating capacity is thermal and 15% hydroelectric mostly from Aswan High Dam.

The thermal power plants represent the main source of thermal pollution. This is due to the low thermal efficiencies of thermal power plants- typically (32-36%). So, according to the second law of thermodynamics a large amount of heat is rejected. This waste heat is removed in the plant condensers through circulating once through cooling water system [1], which is often discharged to a nearby natural body of water such as rivers, lake, or coastal water. This heat increases the water temperature, the excess temperature decreases the dissolved oxygen inside the water and increases the respiration and the

heart beat rate of fish thus decreasing the metabolism process and leading to the death of aquatic life. The excess temperature slows the metabolic reaction as it acts like an inhibitor. On the other hand, the rate of any chemical reaction is doubled by raising the temperature by 10 °C thus affecting the overall productivity of water species.

Discharging the hot water can be achieved either by surface or submerged discharge as shown in Fig. 1. This study is concerned with the deep water in surface discharge specially the near field region where the momentum force is dominant [2], the ambient water is said to be deep where the jet is free to mix due to entrainment and buoyancy and is not constrained by the bed. It can be noted that the deep water may be defined according to the following relation, [3]:

$$\frac{h_{max}}{H} < 0.75 \quad (1)$$

Where:  $h_{max}$  = the maximum depth that the plume will reach if unhindered by the bottom and is equal to  $(0.42F_o A_s^{1/4} \sqrt{h_o b_o})$ ,

H = water depth in the river,

$F_o$  = Densimetric Froude Number,

$A_s$  = aspect ratio  $h_o / b_o$ ,

$h_o$  = outfall depth and  $b_o$  = half width of outfall.

Fig. 2 Sketch shows some parameters used in the study.

From the above, it could be concluded that the most effective dimensionless variables are cross-flow ratio ( $R = \frac{U_a}{U_o}$ ) where  $U_o$  is the thermal discharge velocity,  $U_a$  is the ambient velocity, aspect ratio ( $A_s = h_o / b_o$ ) which is the ratio of the outfall water depth ( $h_o$ ) and half of the outfall width ( $b_o$ ), and  $F_o$  is the Densimetric Froude Number

$$F_o = \frac{u_o}{\sqrt{\frac{\Delta\rho}{\rho} gh_o}}$$

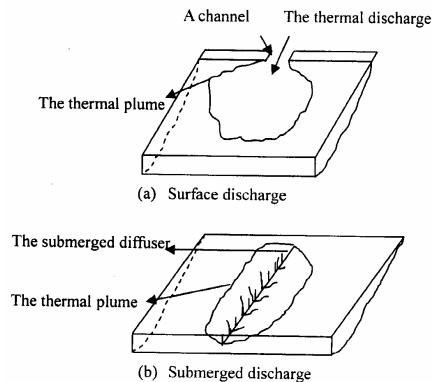


Fig. 1 Ways of thermal discharges, Miller and Brighthouse

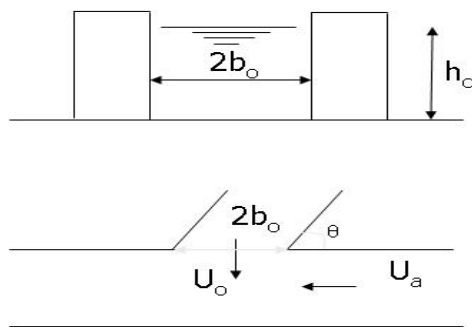


Fig. 2 Sketch shows some parameters used in the study

## 2. DATA of SOME POWER PLANTS in EGYPT

Thermal discharge, temperature, and aspect ratios of some power plants in Egypt are shown in Table (1). It is clear that the aspect ratios ( $A_s$ ) range between 0.15 and 2. The temperature difference between the hot discharge temperature and ambient water temperature ( $\Delta T_o$ ) ranges between 8 °C and 10°C. The discharge ratios ( $Q_o/Q_a$ ) range between 0.09 and 0.839.

In this study it is considered the ambient discharge of the winter closure period in Egypt, where the ambient velocity is the lowest. This is the critical case, where the thermal power plants discharge hot water at very low ambient velocities. The different factors of the experimental program were selected according to the data in Table (1), thermal discharge, temperature, and aspect ratios of some power plants in Egypt, Hydraulics Research Institute (HRI), [4] to [11].

Table 1 Data of some power plants in Egypt

Power plant name	Angle of outfall	Hot disch. m <sup>3</sup> /s	Ambient disch. m <sup>3</sup> /s	Disch. Ratio	Hot disch. temp. °C	Aspect ratio
Cairo West	60°	56.90	630	0.09	9.6	2
Cairo South	60°	58.34	525	0.111	9.6	1.07
El-Kureimat	60°	80.00	183	0.437	9.6	0.82
Cairo North	60°	27.20	35	0.777	8	0.6
New Nubaria Modules I & II	60°	26.00	31	0.839	10	0.15
New Nubaria Module III	30°	21.60	60	0.36	10	0.476
El-Tebeen module I	60°	20.00	1147	0.017	9.3	0.3
El-Tebeen module II	30°	26.00	1147	0.022	8-10	0.223

### 3. STUDY OBJECTIVE

The majority of the studies of the thermal plume size were carried for the thermal discharge into shallow water. On the other hand deep water did not have the same intensity. So, the main objective of this study is to develop empirical formulae for surface discharge of different outfall orientation to predict the thermal plumes center-line length.

### 4. EXPERIMENTAL PROCEDURE

In order to accomplish the study objective, a flume with 17.8 m total length, 2.5 m width and 0.5 m depth was built in HRI. This was chosen with scale modeling satisfying Reynolds Number and Froude Number, to cover the boundary conditions and constrained with the facility of the place in HRI. The feeding system is shown in Fig. 3. In any test group, the experiments proceeded as follows:

1. The flume is divided into 30 cross-sections which are distributed at different distances that are marked and fixed for all runs as shown in Fig. 4.
2. Twenty five sensors are firstly calibrated and mounted on a bridge at equal distances 10 cm apart. The coordinates of the sensors are measured related to a fixed point.
3. To measure the temperature at different levels, the bridge is mounted on a holder which facilitate the up and down movement every 2 cm.

Data analyzing proceeded as the following:

- The temperature difference ( $\Delta T = (T_i - T_c)$ ), was plotted in contours (isotherms) as in Fig. 4. Where  $T_i$  is the water temperature measured by sensors and  $T_c$  is the ambient water temperature in the well.
- The plotted contours for every case then were exported into Autocad program, where the center line lengths of different contours were measured as in Fig. 5.
- The data was arranged in excel sheets then entered to a data fit computer program to get the relations for thermal plume center line length.
- At last, verify these equations on study cases and draw charts for the measured data and the expected data by equations.

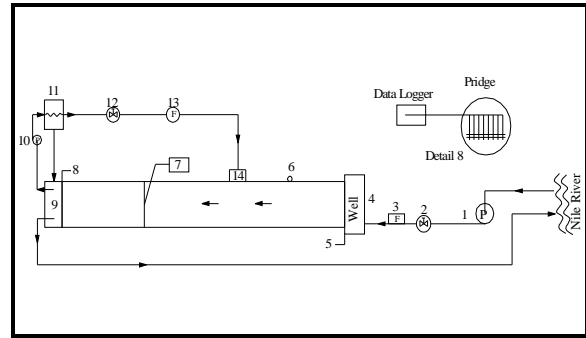


Fig. 3 Feeding process system

- 1 Centrifugal pump
- 2 Gate valve
- 3 Electro magnetic flow meter
- 4 Well
- 5 Weir
- 6 Water level gage
- 7 Bridge having 25 temp. sensors
- 8 Water level adjustment gate
- 9 Well for collecting water.
- 10 Centrifugal pump.
- 11 Electric heater.
- 12 Gate valve.
- 13 Ultra sonic flow meter
- 14 Hot discharge sump.

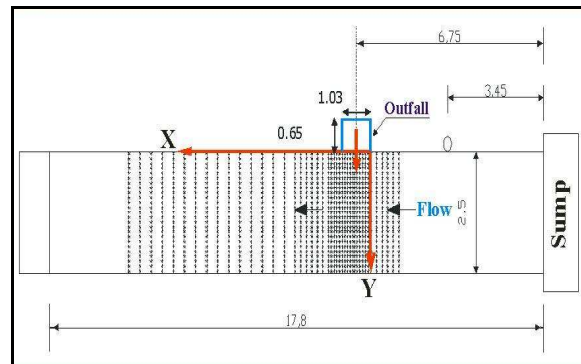


Fig. 4 Sensors location in the flume (Dims in m)

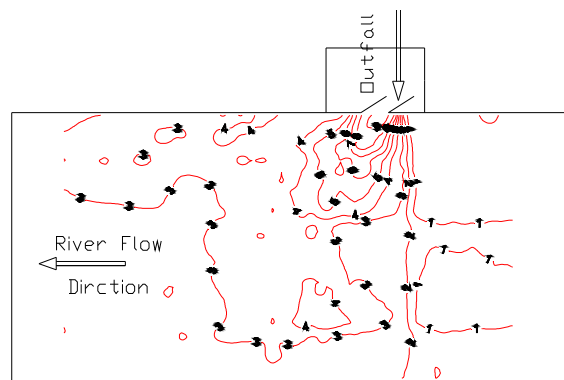


Fig. 5 Temperature contour lines show the thermal plume

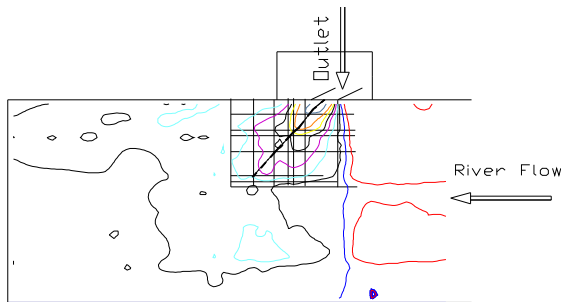


Fig. 6 shows the center line of the thermal plumes

## 5. EXPERIMENTAL INVESTIGATION

### 5.1 Test Program

Based on the real data in Egypt, four values of aspect ratios (1, 1.2, 1.4, and 1.6) were considered, and four values of the cross flow ratio (0.1, 0.2, 0.3, and 0.4) were selected, in this work. Aspect ratio, cross flow ratio, and outlet angle are tested individually in different test runs keeping other factors constant. These arrangements were repeated for three outfall angles (30°, 60°, and 90°) as in Fig. 7.

The temperature difference between the ambient and the hot discharge  $\Delta T = 10^\circ\text{C}$  is taken constant all over the work. Also the ambient water depth is kept 0.3m. The channel width is 2.5m.

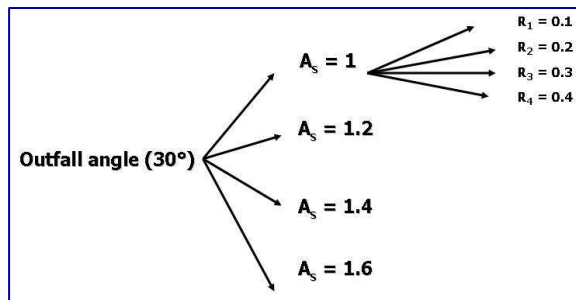


Fig. 7 shows test program at one of outfall orientation

### 5.2 Developing Formulae of the Mixing Zone Center-Line Length

The measured data was analyzed to calculate the mixing zone center-line distance, to have the dimensionless empirical formulae.

The data fit computer program was used to develop the relation between the center-line temperature distance and cross-flow ratio, Froude Number, and aspect ratio. The center line is defined as the center line of the thermal plumes.

Several equations defining the mixing zone center-line temperature distance are available. Among these is the formula of Millar and Brighthouse, [3]. This equation determines the center-line temperature distance in deep water. This equation is a function of Froude Number and aspect ratio at outfall

angle of 90° in stagnant water which mean no cross flow ratio. Miller's and Brighthouse equation is:

$$\frac{s}{\sqrt{h_o b_o}} = (1/2.659 \frac{\Delta T}{\Delta T_o} A_s^{0.253} F_o^{0.052})^{-1.815} \quad (2)$$

#### 5.2.1 Developing a formula for the center line length at outfall angle 90°

In the present study the tests were conducted at outfall angle 90° to develop a formula having the same parameters Froude Number ( $F_o$ ), aspect ratio ( $A_s$ ), cross flow ratio ( $R$ ) and condition of outfall angle 90° as Miller's equation, [1]. The measured data was analyzed to calculate the mixing zone center-line distance to have the following dimensionless empirical formula:

$$\frac{s}{\sqrt{h_o b_o}} = (1 - \text{Exp}(\frac{\Delta T}{\Delta T_o}) / \text{Exp}(1)) \text{Exp}(aR + bA_s F_o + (1 - \frac{\Delta T}{\Delta T_o})c + d) \quad (3)$$

Where:  $a = -0.1994$ ,  $b = -0.1688$ ,  $c = 0.8121$  and  $d = 4.694$ .

Miller's equation and the present equation were used to calculate the center-line of thermal plumes of the same power station, Stolzenbach and Harleman power station in Michigan [1]. Fig. 8 shows a comparison between the measured and predicted data by Miller's equation and the present developed equation for Stolzenbach power station. It could be noticed that the developed formula fits more the measured data than Miller equation in the range before  $\Delta T / \Delta T_o = 0.35$ , after that range Miller's equation fits more than the developed equation. This means that the developed equation gives a good prediction for center-line length for a certain range of temperature difference ( $\Delta T / \Delta T_o > 0.35$ ) which is the range of temperature difference of 4 to 10 °C for this study.

#### Sensitive analyses of the cross flow ratio

Figure 9 shows that the cross flow ratio ( $R$ ) has an effect on the mixing zone center line. On the other hand, increasing  $R$  in open channels increasing the cooling efficiency and decreasing the mixing zone center line distance. Miller's equation could be applied only in the case of stagnant water and did not consider moving water. In that case, the developed equation with the effect of  $R$  could be applied.

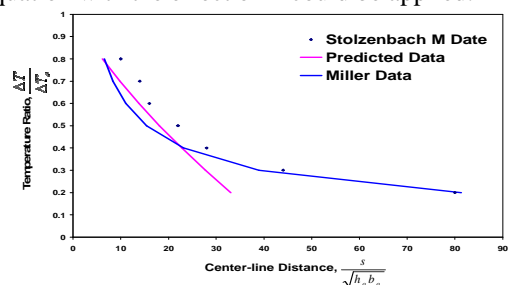


Fig. 8 Comparison between the measured data and predicted by developed and Miller's formulae of Stolzenbach power station

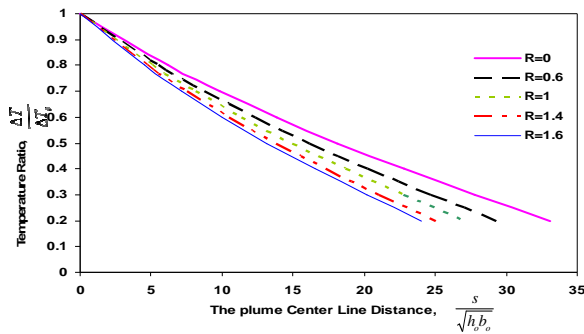


Fig. 9 Effect of the change of cross flow ratio on the thermal plume center line

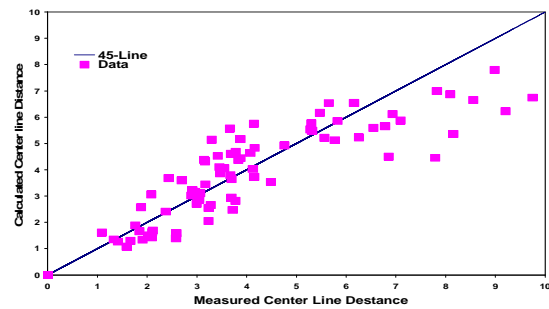


Fig. 11 The deviation between measured and calculated data for outfall angle 30°

### 5.2.2 Developing formula for the center line length at outfall angles 60° and 30°

More tests were conducted at the model with outfall angles 60° and 30°. The measured data was analyzed to calculate the mixing zone center-line distance, to have the dimensionless empirical formulae for the two outfall angles (30°, 60°). The dimensionless formula for 30°-outfall angle is as follows:

$$\frac{s}{\sqrt{h_0 b_0}} = (1 - \text{EXP}(\frac{\Delta T}{\Delta T_0}) / \text{EXP}(1)) \text{EXP}(aR + (A_s F_0)^b - c) \quad (4)$$

Where;  $a=2.258$ ,  $b=0.873$  and  $c=-1.26$

While the dimensionless formula for 60°-outfall angle is as follows:

$$\frac{s}{\sqrt{h_0 b_0}} = (1 - \frac{\Delta T}{\Delta T_0})^a (\text{EXP}(bR + cA_s + dF_0 + e)) \quad (5)$$

Where  $a$ ,  $b$ ,  $c$ ,  $d$ , and  $e$  are constants equal to 0.856, -1.696, -0.856, -0.103 and 4.293 respectively.

Equations (4) and (5) are applied within the present ranges of experiments. They have a deviation of about 10.5% and 12% respectively. Figs. 10 and 11 show the deviation of center line distance between measured and calculated data for outfall angles 60° and 30°.

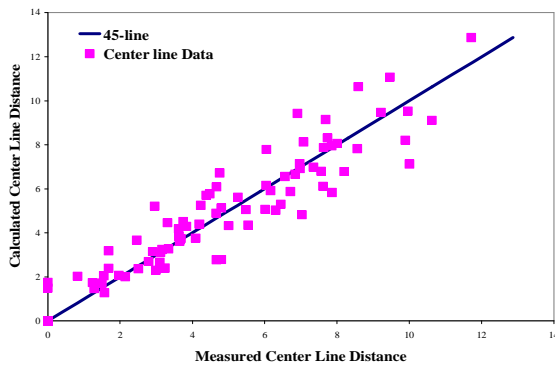


Fig. 10 The deviation between measured and calculated data for outfall angle 60°

### Verification of developing formula for the center line length at outfall angles 60° and 30°

The obtained formulae were verified the data of El-Tebeen Power Plant in Egypt with its two modules, as the following:

Outfall angle	$\Delta T$	R	$A_s = h_0/b_0$	$F_0$
60°	9	1	0.3	0.5651
30°	8	0.784	0.223	6.44

Equations (4) and (5) were applied and Figs. 12 and 13 shows the comparison between the predicted center-line temperature distances of the thermal plumes by the present developed formulae and El-Tebeen data. It is clear that the results of developed equations are in good agreement with the measured data

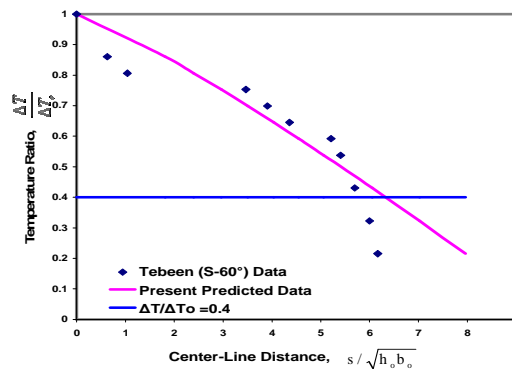


Fig. 12 Results of developed Eq. and El-Tebeen data for 60° outfall angle

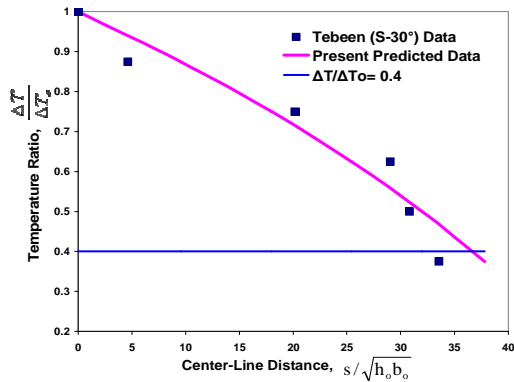


Fig. 13 Results of developed Eq. and El-Tebeen data for 30° outfall angle

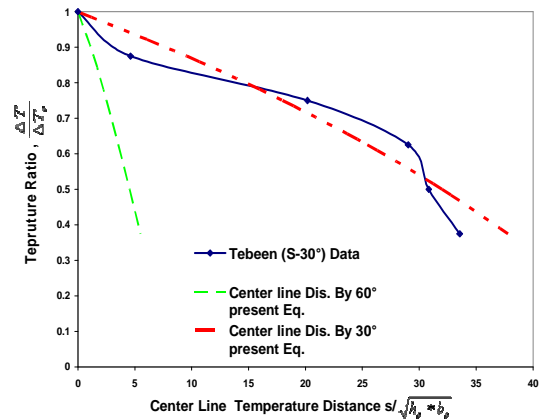


Fig. 15 Comparison between the predicted mixing zone center line temperature distance calculated by 60° and 30° analytical model against the measured data of El-Tebeen 60°

### 5.3 Sensitivity of the outfall orientation on the center line length

A good agreement was observed between the expected center line by the developed formula of 60° outfall angle and the measured data of El-Tebeen (60° outfall angle), while the developed equation of 30° outfall angle have considered deviation as shown in Fig. 14. Fig. 15 shows a Comparison of mixing zone center line calculated by 60° analytical model and 30° analytical model against El-Tebeen (30° outfall) field data. A good agreement was observed between the expected center line by the developed formula of 30° outfall angle and the measured data of El-Tebeen (30° outfall angle), while the developed equation of 60° outfall angle have big deviation. Which mean that the outfall angle has an effect on the mixing zone center line distance.

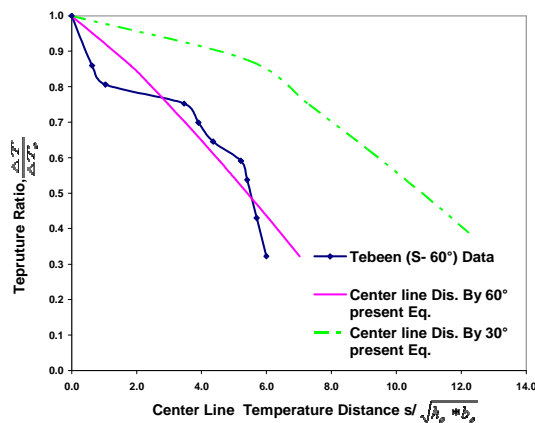


Fig. 14 Comparison between the predicted mixing zone center line temperature distance calculated by 60° and 30° analytical model against the measured data of El-Tebeen 30°

## 6. CONCLUSIONS

From the present investigations the following could be concluded:

- 1) The developed formula for center line length for certain temperature difference could predict the center line length as Miller's equation.
- 2) The factor (R) improved the results of the developed equation and gave the variety of using it in stagnant and moving water.
- 3) The outfall angle influences the thermal plume center-line length. This was detected while comparing the predicted data from the developed formulae at 30° and 60°. Every equation suits its conditions only.

In general it is concluded that the developed equations for mixing zone center-line length, could be a good tool in prediction the thermal plume size. Also these predicted formulae could help in updating the Environment and Water Legislations in Egypt and other countries having the same conditions.

## 7. RECOMMENDATIONS

The following recommendations could be considered in the future work:

- 1) More studies are to be conducted to determine the relation between Froude number and aspect ratio and cross flow ratio and their influence on the thermal plume size.
- 2) More studies are needed to be conducted to establish relations that could calculate the dimensions of the mixing zone for wider range of temperature difference ratios.

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